



# A S-N-based Cohesive Element for Delamination Propagation in Composite Materials

Ανάπτυξη Συνεκτικών Στοιχείων (Cohesive Elements) Βασισμένων σε Αποτελέσματα Καμπυλών Κόπωσης S-N για την Μοντελοποίηση Διαστρωματικής Αποκόλλησης σε Σύνθετα Υλικά

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Diploma Thesis

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## OBJECTIVE

Delamination in composites is accompanied by complex damage mechanisms such as fiber bridging and matrix cracking. These mechanisms increase the critical energy release rate,  $G_c$ , required to propagate the crack. This increase in  $G_c$  when plotted against the crack extension  $\Delta a$  is referred to as the resistance curve (R-curve).

An experimental study was conducted by Yao<sup>1</sup> to quantify the significance of fiber bridging in the delamination growth in multidirectional composite laminates by comparing quasi-static and fatigue R-curves.

The objective of this thesis was to verify the capabilities of a recently proposed cohesive fatigue damage model<sup>2</sup> by comparing the numerical predictions of Yao's experiments to the test data.

## Cohesive Zone Model

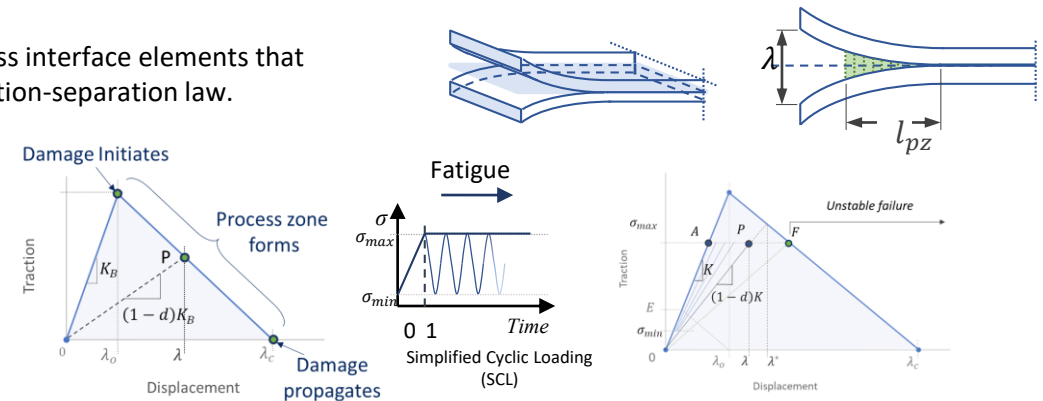
Cohesive elements, are zero thickness interface elements that represent the separation with a traction-separation law.

### Fatigue Damage model:

- Same damage envelope for QS and fatigue
- Based on normalized S-N Curve
- Damage accumulates at rate dictated by a function:

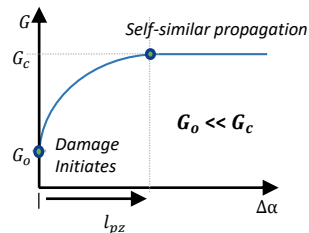
$$\frac{dD}{dN} = C \left( \frac{\lambda}{\lambda^*} \right)^\beta$$

The CZM is implemented in a UMAT in Abaqus for FE analysis

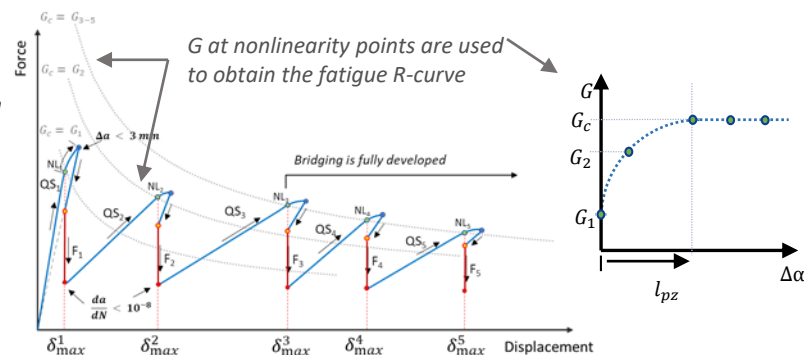


## R-Curves

### Quasi-static fracture:



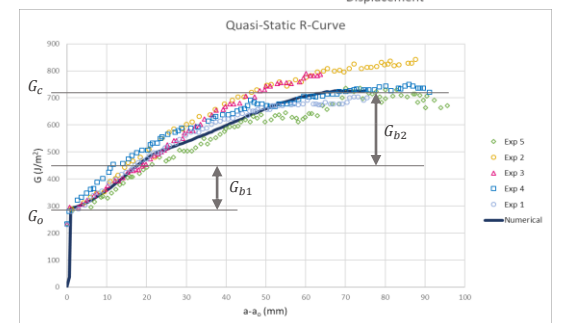
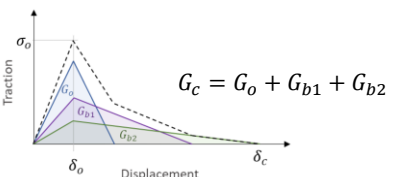
### Fatigue fracture: Experimental procedure described by Yao



## MAIN WORK

- Programmed a UMAT user-written subroutine of Dávila's model.
- Developed an FEM model of a double cantilever beam specimen.
- Performed analyses for:
  - QS characterization of interfaces (QS R-curve)
  - Fatigue propagation rates and R-curve modeling for R=0.1 and R=0.5

### Quasi-static characterization:



## CONCLUSIONS & FUTURE WORK

The numerical results indicate that:

- The Quasi-Static (QS) and Fatigue R-curves can be modeled using a superposition of cohesive laws and the proposed CZM.
- The Paris Law for short cracks (exponent and pre-factor) can be accurately predicted.

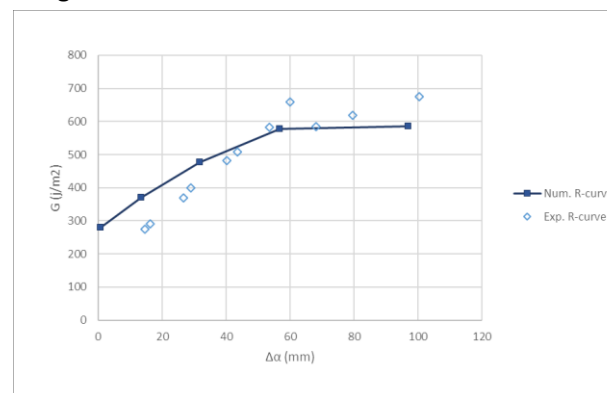
### Future work:

As errors are observed for longer crack extensions, it is proposed to:

- Verify the effect of Quasi-static (QS) characterization of the R-curve on the errors
- Evaluate the effect of the Fatigue mode's parameters on the errors

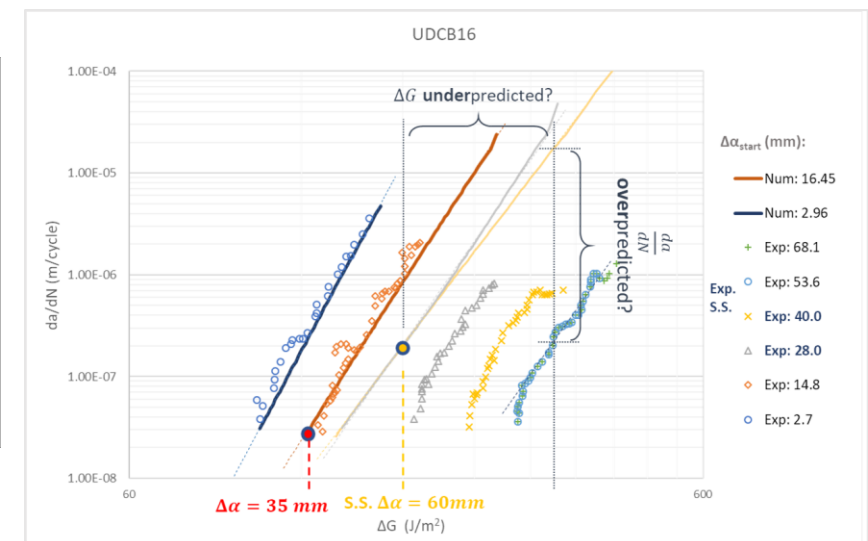
## Fatigue results:

### Fatigue R-curve:



Overprediction of  $G_c$  for short crack extensions VS Underprediction of  $G_c$  for longer crack extensions

## Typical propagation rate results:



[1] Yao, L., Alderliesten, R., Zhao, M., and Benedictus, R., "Bridging Effect on Mode I Fatigue Delamination Behavior in Composite Laminates," *Composites Part A: Applied Science and Manufacturing*, Vol. 63, 2014, pp. 103-109.

[2] Dávila, C. G., Rose, C. A., Murri, G. B., Jackson, W. C., and Johnston, W. M., "Evaluation of Fatigue Damage Accumulation Functions for Delamination Initiation and Propagation," *Technical Publication NASA/TP-2020-220584*, Hampton, VA, April 2020.